

6 Exponential Regression using Microsoft Excel

7 Method: This method uses Excel's tool for regression analysis which determines the slope and intercept of straight line data.
 8 An exponential equation has the general form: $y = be^{mx}$
 9 Taking the natural log of both sides of the equation yields the equation: $\ln(y) = mx + \ln(b)$
 10 The equation above is the equation of a straight line with y on a log scale and x on a linear scale.
 11 Regression analysis performed on the x data and the $\ln(y)$ data will yield the slope, m, and the intercept, $\ln(b)$.
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 13 Problem 3.18 - Plot C vs W and use regression to find an exponential formula of the form $y = be^{mx}$ (or $C = be^{mW}$)
 14 Geiger Counter: Counts per second vs plate thickness

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 16 Measured data from textbook:

Plate Thickness W (mm)	Geiger Counter C (counts per second)
2.0	5500
5.0	3700
10.0	2550
20.0	1300
27.5	715
32.5	470

Extra column
for regression:

$\ln(C)$
8.613
8.216
7.844
7.170
6.572
6.153

Regression data for
straight line on graph:

$C = be^{mW}$
5018.4
3981.5
2707.2
1251.6
701.8
477.2

formula: =B\$47*EXP(B\$43*A19)

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 26 SUMMARY OUTPUT

<i>Regression Statistics</i>	
Multiple R	0.997902337
R Square	0.995809075
Adjusted R Square	0.994761344
Standard Error	0.069589815
Observations	6

Perform exponential regression as follows:

1. Form a column for $\ln(y)$ data - see above
2. Select Tools - Data Analysis - Regression from the menu (see Note below)
3. Use the x values for the independent variable and the $\ln(y)$ values for the dependent variable. For the output range, specify the cell location for the upper left corner of the report.

Note: If Data Analysis is not listed under the Tools menu, first select Tools - Add-ins - Analysis Tool Pack

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 35 ANOVA

	df	SS	MS	F	ignificance F
Regression	1	4.60275	4.60275157	950.4432	6.6E-06
Residual	4	0.01937	0.00484274		
Total	5	4.62212			

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	Coefficients	Standard Er	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	8.675157247	0.04943	175.486447	6.33E-09	8.537904	8.812411	8.537904	8.812411
X Variable 1	-0.07714813	0.0025	-30.8292587	6.6E-06	-0.084096	-0.0702	-0.084096	-0.0702

$\ln(b) = 8.675157247$ Note: From cell B30, R Square = 0.995809 **Good fit!**

so $b = e^{\ln(b)}$

or $b = 5855.6$

$m = -0.0771$

so $y = be^{mx}$ or

$C = 5856e^{-0.0771W}$

Form an xy graph using W = x-axis series, C = 1st series, and $C = be^{mW}$ data = 2nd series.

Use a log scales for the y-axis and a linear scale for the x-axis. The data should fall in a straight line.

Show points only for the 1st series and line only for the 2nd series.

